

# General Certificate of Secondary Education November 2010 

Mathematics<br>4306<br>Specification A<br>Paper 2 Foundation

## Final

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

[^0]Set and published by the Assessment and Qualifications Alliance.

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

M Method marks are awarded for a correct method which could lead to a correct answer.

A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.

B Marks awarded independent of method.
Mdep A method mark dependent on a previous method mark being awarded.
B dep A mark that can only be awarded if a previous independent mark has been awarded.
ft Follow through marks. Marks awarded following a mistake in an earlier step.

SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
oe Or equivalent. Accept answers that are equivalent. eg, accept 0.5 as well as $\frac{1}{2}$

| Q | Answer | Mark | Comment |
| :---: | :---: | :---: | :---: |
| 1 (a) | $56 \div 100 \times 250$ | M1 | 140 |
|  | $£ 1.40$ or $£ 140$ p or $£ 1.40$ p | A1 | $£ 140$ is M1A0, $£ 1.4$ is M1A0 |
| $1 \text { (b) }$ | 3 | B1 |  |
| 2 (a) | 75040 | B1 | Allow 75,040 but B0 for 75.040 |
| 2 (b) | nine thousand (and) eight | B1 | Nine, thousand eight Allow poor spelling |
| 3 (a) | 25 | B1 |  |
| 3 (b) | $\frac{2}{10}$ | B1 |  |
| 3 (c) | $\frac{10}{20}$ | B1 |  |
| 4 (a) | 1997 | B1 | Ignore any , or |
| 4 (b) | 1954 | B1 | Ignore any, or |
| 4 (c) | 1989-40+60 | M1 | 1949 |
|  | 2009 | A1 | Ignore any , or |
| 5 (a) (i) | 15 - half of 6 or $24 \div 2$ | M1 | $30-6 \div 2$ is M0 unless recovers to correct answer |
|  | 12 | A1 |  |
| 5 (a) (ii) | 15 | B1 |  |
| 5 (b) | 4 | B2 | B1 for 26 or 56 seen Allow embedded answers unless contradicted on answer line when B1 |
| 6 (a) | $(5,3) \text { or }(x=5, y=3)$ <br> Answer may be on diagram | B1 | B0 for ( $x 5, y 3$ ), B0 for ( $5 x, 3 y$ ) |
| 6 (b) | 4 answer may be on diagram | B1 | 0.4 is B0 |
| 6 (c) | Answer to (6b) ${ }^{2}$ | B1ft | 16 |
| 6 (d) | $(3,5) \text { or }(x=3, y=5)$ <br> Answer may be on diagram | B1 | B0 for ( $x 3, y 5$ ), B0 for ( $3 x, 5 y$ ) |


| Q | Answer | Mark | Comment |
| :---: | :---: | :---: | :---: |
| 7 |  | B3 | B2 3 correct <br> B1 1 or 2 correct |
| 8 | RH, BH, GH, RT, BT, GT, and/or reversed or small letters | B2 | -1 each error or omission |
| 9 (a) |  | B1 | Ignore any hidden edges if shown. <br> Allow rectangle or parallelogram for base, but at least two faces must look like a square or a rhombus. <br> Allow approximately parallel edges Edges can be freehand B0 for net of a cube |


| $\mathbf{9}(\mathbf{b})$ | tetrahedron | B1 |  |
| :--- | :--- | :--- | :--- |


| $\mathbf{1 0}(\mathbf{a})$ | 35 | B1 |  |
| :--- | :--- | :--- | :--- |
| $\mathbf{1 0}(\mathbf{b})$ $6 \times(9-7)+3$ B1  |  |  |  |


| $\mathbf{1 0}(\mathbf{c})$ | $(3+2) \times(5+6)$ | B1 |  |
| :--- | :--- | :--- | :--- |


| $\mathbf{1 1}(\mathbf{a})$ | none or 0 | B1 | zero oe |
| :--- | :--- | :---: | :--- |
| $\mathbf{1 1}(\mathbf{b})$ parallelogram B1 Allow any spelling <br> but not just 'parallel' |  |  |  |


| $\mathbf{1 1}(\mathbf{c})$ | Any correct obtuse angle <br> Need not be labelled provided it is <br> unique | B1 | May be interior or exterior angle |
| :---: | :--- | :---: | :--- |


| $\mathbf{1 1}$ (d) | 6.3 to 6.5 cm | B1 | 63 to 65 mm may be on diagram |
| :---: | :--- | :--- | :--- |


| $\mathbf{1 1}($ e) | $52^{\circ}$ to $54^{\circ}$ | B1 | May be on diagram |
| :--- | :--- | :--- | :--- |




B1 for any correct pair with no extras.
Or can use centre square + any other
B1 B0 eg and their rotations


| (c) | $\begin{array}{l}\text { isosceles triangle has no rotational } \\ \text { symmetry } \\ \text { It has rot. symmetry of order 1 }\end{array}$ | B1 | $\begin{array}{l}\text { This describes an equilateral triangle . } \\ \text { Because the sides are not all the same. } \\ \text { The angles are not all the same. } \\ \text { (only)two sides are the same. } \\ \text { (only)two angles are the same. }\end{array}$ |
| :--- | :--- | :---: | :--- |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
| symmetry of order 2 |  |  |  |$]$


| $\mathbf{1 3}$ (a) | -9 | B1 | B0 for 9 |
| :--- | :--- | :---: | :--- |
|  | 26 | B1 | B0 for -26 |


| $\mathbf{1 3}$ (b) | -14 | B1 |  |
| :--- | :--- | :--- | :--- |


| 14 (a) |  | B1 |
| :---: | :---: | :---: |


| $\mathbf{1 4}$ (b) | 15 | B1 |  |
| :--- | :--- | :---: | :--- |
|  | Their $15+4$ | B1ft | 19 |


| Q | Answer | Mark | Comment |
| :---: | :--- | :---: | :--- |
| $\mathbf{1 4}$ (c) | Add 4, +4, plus 4, <br> number of sticks + 4. <br> miss out the next odd number and then <br> go to the next odd number | B1 | $4 n-1$ oe allow use of other letter <br> Allow $n 4-1$ <br> B0 for $n=+4, n+4$, number + 4 <br> $n=4 n-1$ etc <br> B0 for correct and incorrect <br> eg +4 and $n+4$ |


| 14 (d) | 31 or 35 seen <br> $4 n-1=32$ has no integer solution. <br> pattern 8 has 31 sticks. <br> one stick left over <br> 3 sticks short | B1 | oe no even numbers, no even terms <br> only odd numbers <br> 32 is an even number |
| :--- | :--- | :---: | :--- |
| B0 because adding 4 each time |  |  |  |
| B0 started at 3 sticks |  |  |  |


| $\mathbf{1 5}$ | Bags $10 \times 2.85$ | M1 |  |
| :---: | :--- | :---: | :--- |
|  | 28.50 | A1 | Allow 28.5 |
|  | Single load $17+10$ | M1 | 27 |
|  | Single load or $£ 27$ or 'delivery' on <br> answer line oe | A1cao | A1 is cao so there must be no errors in the <br> working |
| $\mathbf{1 5}$ ALT | $25 \div 2.85$ and $250 \div 27$ oe | M1 | $2.85 \div 25$ and $27 \div 250$ oe |
|  | $8.77(\mathrm{~kg} / £)$ or 8.8 | A1 | $0.114(£ / \mathrm{kg})$ |
|  | 9.26 or 9.3 | A1 | 0.108 |
|  | Single load or $£ 27$ or 'delivery' on <br> answer line oe | A1cao |  |


| 16 (a) | $9 a$ | B1 | B0 for $7 a+2 a$ <br> Penalise further work eg $9 a=a^{9}$ is B0 |
| :---: | :---: | :---: | :---: |
| 16 (b) | $7 a-8 f+6 a+5 f$ | B2 | B1 for $-8 f$ or ++- or -+- |
| 17 (a) | 49, 64, 81 | B2 | B1 for any 2 of these or any other square numbers |
| 17 (b) | $49+25+9+1$ | M2 | M1 for any 3 of these but must be no even square numbers |
|  | 84 | A1 | SC1 for eg $84 \times 4,84 \times 6,84^{3}$ etc after seeing 84 |


| $\mathbf{1 8}$ | Stating sides are 12108 cm <br> May be on drawing in question | B1 | Can be implied if diagram is correct |
| :---: | :--- | :---: | :--- |
|  | Two sides drawn to 3 mm accuracy | M1 |  |
|  | All 3 sides correct and a triangle | A1 |  |


| $\mathbf{1 9}$ (a) 7 | B1 |  |
| :--- | :--- | :---: | :--- |


| 19 (b) 8 | B1 |  |
| :--- | :--- | :--- | :--- |


| 19 (c) 6 | B1 |  |
| :--- | :--- | :--- | :--- |


| Q | Answer |  | Mark |
| :---: | :--- | :---: | :--- |
| $\mathbf{1 9}$ (d) | Attempt at $\sum x f$ <br> $12+5+12+56+48+45+50$ <br> $(=228)$ | M1 | $4 \times 3+5 \times 1+\ldots+10 \times 5$ <br> Allow one arithmetic error or omission of a <br> product |
|  | Their $228 \div 30$ | M1Dep | $12+5+\ldots+50 \div 30$ is M1M0 unless <br> recovers |
|  | 7.6 | A1 | Allow 7 or 8 after 7.6 or 228 $\div 30$ seen |


| $\begin{gathered} 19 \text { (d) } \\ \text { ALT } \end{gathered}$ | $4+4+4+5+6+6+\ldots+10+10$ | M1 | Allow one missed value |
| :---: | :---: | :---: | :---: |
|  | Their $228 \div 30$ | M1Dep |  |
|  | 7.6 | A1 | Allow 7 or 8 after 7.6 or $228 \div 30$ seen |


| 20 (a) | $(0) .612244898$ | B1 | $(0) .6122449$ |
| :--- | :--- | :--- | :--- |


| 20 (b) | $(0) .6$ | B1ft | Round their answer to 1sf |
| :--- | :--- | :--- | :--- |


| 21 | Use mark scheme on LHS or RHS whichever is most beneficial to candidates |  |  |
| :---: | :---: | :---: | :---: |
|  | A pair of numbers that satisfy condition one eg | M1 | $b-1=s+1$ or $b+1=2(s-1)$ |
|  | A pair of numbers <br> condition two satisfy <br> col two <br> Sal     <br> Sal 3 4 6  <br> Bill 1 3 5 9 | M1 | Both equations |
|  | $\mathrm{Sal}=5, \mathrm{Bill}=7$ | A1 | Correct answer gets 3 marks <br> Can score M0M1A0 <br> Sc 2 for Sal 7 Bill 5 |


| $\mathbf{2 2}(\mathbf{a})$ | $5.6 \times 3.7$ | M1 |  |
| :--- | :--- | :---: | :--- |
|  | $20.7(2)$ | A1 | 20.75 is M1A0 |


| 22 (b) | 18.6 | B1 | 18.60 |
| :--- | :--- | :--- | :--- |


| $\mathbf{2 3}$ | Sight of 1.18 | B1 |  |
| :---: | :--- | :---: | :--- |
|  | $1.18 \times 145$ | M1 |  |
|  | 171.10 | A1 | 171.1 is A0 |


| Q | Answer | Mark | Comment |
| :---: | :---: | :---: | :---: |
| $\begin{gathered} 23 \\ \text { ALT } \end{gathered}$ | $\frac{18}{100} \times 145(26.1)$ | M1 | Allow build up method for $18 \%$. Must get to $18 \%$ but allow arithmetic errors for M1 |
|  | $145+$ their 26.1 | M1dep | $\frac{118}{100} \times 145 \mathrm{M} 2$ |
|  | 171.10 | A1 | 171.1 is A 0 |

$\left.\begin{array}{|c|l|c|l|}\hline \text { 24 (a) } & \begin{array}{l}\text { 'Either' ticked and prime can be odd or } \\ \text { even stated or shown } \\ \text { Needs both parts for one mark }\end{array} & \text { B1 } & \begin{array}{l}\text { Allow misreads of formula as } p r \text { or }(p r)^{2} \text { or } \\ \text { miscalculations as long as } \\ p=2 \text { and } p=\text { odd prime mentioned }\end{array} \\ \text { eg } 2 \times 3^{2}=36 \text { and } 3 \times 3^{2}=81\end{array}\right]$

| $\mathbf{2 4}$ (b) | Any valid expression, eg $x y+z$ <br> Must use all 3 letters | B1 | Allow numbers if all variables used, <br> ie $x+y+z+1,2(x+y+z)$ <br> B0 for $x \pm y \pm z$ |
| :---: | :--- | :---: | :--- |


| $\mathbf{2 5}$ | $800+1200+1400+700(=4100)$ | M1 | Allow 1 arithmetic error |
| :---: | :--- | :---: | :--- |
|  | $2 \times$ their $4100(=8200)$ | M1 |  |
|  | $\frac{130}{360} \times$ their 8200 | M1Dep | Dependent on first M1 then doubling or <br> halving their 4100 <br> eg $130 \div 360 \times 2050$ is M1 <br> Accept $36 \%$ of their 8200 oe <br> $130 \div 180 \times 4100$ is M3 |
|  | 2950 to 2965 | A1 | SC1 2800 or $2 \times 1400$ |


| $\mathbf{2 6}$ | $16 \times 4(=64)$ | B1 |  |
| :---: | :--- | :---: | :--- |
|  | $\pi \times 8^{2} \div 2$ | M1 | $\pi \times 16^{2} \div 2(400.92$ to 402.18), <br> $\pi \times 6^{2} \div 2(56.52$ to 56.56$)$ |
|  | 100.48 to 100.57 | A1 | $32 \pi$ |
|  | 164.48 to 164.57 <br> 164 or 165 with working | A1ft <br> ft if an area of a rectangle calculated with a <br> length of 16 and any other width <br> eg 152.52 to 152.56 comes from using 6 as <br> radius and height and so scores 2/4 |  |


| $\mathbf{2 7}$ | $250 \div 8 \times 5$ or $250 \div 8 \times 3$ | M1 |  |
| :--- | :--- | :---: | :--- |
|  | 156.25 and 93.75 | A1 | or reversed |


| $\mathbf{2 8}$ (a) | High | B1 |  |
| :--- | :--- | :--- | :--- |


| Q Answer | Mark | Comment |
| :---: | :---: | :---: | :---: |
| $\mathbf{2 8}$ (b) 30 B1  |  |  |

$\mathbf{2 8}$ (c)

| $\mathbf{2 9}$ | $2 x<8$ or $2 x<6$ | M1 | $2 x \leq 8$ |
| :--- | :--- | :---: | :--- |
|  | $x<4$ or $4>x$ | A1 | $x<4$ in working but just 4 on answer line <br> gets M1A0 |


| 30 (a) | Correct plots at mid class point to 1 <br> square accuracy and joined up <br> Ignore any extra lines going back to <br> horizontal axis at start or end | B2 | B1 7 correct plots but not joined up <br> B1 5 or 6 correct plot at midpoints <br> to 1 square accuracy and joined up <br> B1 7 correct plots at upper or lower class <br> boundaries and joined up <br> B0 for bar chart only, but mark frequency <br> polygon if seen as well |
| :---: | :--- | :---: | :--- |


| 30 (b) | Any correct statement using both sets of data. This is not a ft mark eg |  |  |
| :---: | :---: | :---: | :---: |
|  | Higher average spend at shop A <br> Lower average spend at shop B <br> Higher mean at A <br> Higher median at A <br> More money spent at A <br> Same number of people spend $£ 80$ to <br> £100 <br> Same number of people spend $£ 20$ to <br> £40 <br> 12 people spend $£ 50$ at A but 18 spend $£ 50$ at B | B1 | More spread out at shop A <br> Less spread out at shop B oe <br> Mode at A higher (than mode at B) <br> Same range <br> More people in B spend $£ 40$ to $£ 60$ <br> More spend $£ 70$ at B <br> 20 shoppers spend $£ 90$ <br> B0 they both go up and down <br> B0 more spend $£ 70$ in one shop than the other <br> B0 A highest was $£ 110$ but B was $£ 70$ |


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